The Bigger Fish:

A Comparison of State-of-the-art QSAR Models on Low-resourced Aquatic Toxicity Regression Tasks

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Abstract

Toxicological information as needed for risk assessments of chemical compounds is often sparse. Unfortunately, gathering new toxicological information experimentally often involves animal testing. Therefore, simulated alternatives, such as Quantitative Structure-Activity Relationship (QSAR) models, that use known toxicity values to infer the toxicity of a new compound, are preferred. Indeed, the European Union allows chemicals emitted into the environment to be registered with aquatic toxicity information via simulated experiments. These aquatic toxicities are calculated by considering the impact of a given chemical on different aquatic species. Aquatic toxicity data collections, thus, consist of many related tasks - each predicting the toxicity of new compounds on a given species. Since many of these tasks are inherently low-resource, i.e., involve few associated compounds, this is a challenging problem. Meta-learning, a subfield of artificial intelligence, enables the utilization of information captured across tasks, leading to more accurate models. In our work, we benchmark various state-of-the-art meta-learning techniques for building QSAR models, focusing on knowledge sharing between species. Specifically, we employ and compare transformational machine learning, model-agnostic meta-learning, fine-tuning, as well as multitask models. Our experiments show that established knowledge-sharing techniques outperform single-task approaches. Based on our results, we recommend the use of multitask random forest models for aquatic toxicity QSAR modelling, which matched or exceeded the performance of other approaches and robustly produced good results in low-resource settings. This model functions on a species level predicting toxicity for multiple species across phyla with flexible exposure duration and on a large chemical applicability domain.

Synopsis: In a bid to reduce animal experiments, we analyse the performance of state-ofthe-art Quantitative Structure-Activity Relationship (QSAR) regression models on sparse aquatic ecotoxicity datasets. Further, the impact of the amount of data to build these models is investigated.

Introduction

With the advent of machine learning, the field of Cheminformatics has flourished by using data science techniques on physical-chemical problems. One such problem is the modelling of the bio-activity related to molecular compounds. Known as Quantitative Structure-Activity Relationship (QSAR) modelling, the field aims to reduce the need for *in vivo* - in organism - and *in vitro* - in test tube - experiments via cost-effective *in silico* simulated approaches. The research in this field has been motivated for decades by the aim of reducing experiments that are expensive in terms of life, cost, and time (see, e.g., Cherkasov et al.¹).

QSAR models relate chemical structures to their biological activity in a given target domain, from full organisms to specific proteins and even to specific genes. The biological activities which QSAR models aim to predict are manifold and domain-specific. Toxicity can be measured by the impact a compound has on the mortality, reproduction, mobility or growth of certain species. Our work specifically addresses the toxicity causing mortality in aquatic species. The prediction of aquatic toxicity as a biological activity has its prevalent use in risk assessment for environmental protection. With the increasing amount of industrial chemicals being used and developed, the European Union Regulation for the Registration, Evaluation, Authorisation and Restriction of Chemical Substances (REACH) requires an investigation into the aquatic toxicity of a chemical released into the environment, for instance through QSAR models.² Due to this regulation, there is a strong need for better-performing aquatic toxicity QSAR models, that predict the toxicity of chemicals on various aquatic species such as water flees (so-called Daphnia), algae and fish.

The scientific community has developed methods that enable sharing of knowledge across datasets; these methods are commonly referred to as *meta-learning*.³ While various definitions of meta-learning have been proposed, in this paper we adopt a definition that views meta-learning in its broadest sense, i.e., learning across a single task. We will discuss and benchmark several methods that fall under this broad definition of meta-learning.

One example would be multitask learning, where multiple tasks are learnt jointly using

a single predictive model, enabling that model to utilise knowledge across tasks.

We believe the use of these techniques could be beneficial in utilising and predicting the many low-resource tasks inherent to aquatic toxicity. We, therefore, investigate stateof-the-art knowledge-sharing approaches to QSAR modelling and apply these methods to a species-level aquatic toxicity model predicting for multiple species across phyla with flexible exposure duration.

In this article, we aim to model the toxicity of many aquatic species individually in a generally applicable model which makes no restrictive assumptions on its chemical input. Considering recent research on meta-learning in QSAR modelling, 10 state-of-the-art models representing recent developments are adapted and applied for aquatic toxicity prediction. Via a dataset collection gathered from ECOTOX, consisting of 24 816 assays, 351 separate species, and 2674 chemicals, we carry out a general comparison of the QSAR models with internal and external validation. We also simulate low-resource situations by artificially down-sampling the datasets to few assays per species, or few species to share knowledge between. We compare single-species models and multi-species models and assess the benefit of using meta-learning techniques. Finally, we provide useful knowledge to future QSAR developers by investigating the impact of low-resourced situations on the modelling techniques, and we recommend QSAR models to use for aquatic toxicity. All our results are made publicly available via a Git repository.⁴

Problem Statement

This section elaborates on the problem of predicting aquatic toxicity tackled in our work and addresses the domain-specific OECD test guidelines that are used to generate the toxicity data used in ecotoxicological risk assessment, and that therefore guide the QSAR model development.

Aquatic Toxicity Problem

With the aim of reducing animal testing, *in silico* tools should be able to predict the toxicity of a compound after a specific exposure duration and for the species that it is tested on. Representing the aquatic ecosystem, regulatory tools may as a minimum provide toxicity levels for three representative groups: 'acute fish toxicity', 'acute daphnid toxicity', and 'alga toxicity'.^{5,6}

We aim to build generally applicable QSAR models that predict the toxicity of chemicals across phyla on a species level using training data of all species; therefore, any meta-learning approach should determine which data from related species should be used in modelling the toxicity of compounds on a target species. Our QSAR models are aimed at having a large applicability domain for compounds, they should be able to produce reasonably accurate predictions across a large variety of chemicals. Many QSAR problems are simplified into binary classification tasks, predicting whether a specific compound is toxic or not via manually chosen thresholds. In contrast, our work builds regression models, which directly predict the real-valued concentration of a chemical at which 50% of a given species dies – the LC50 (Lethal Concentration 50% mortality) endpoint.

Furthermore, we predict toxicities across variable exposure durations. Our model thus predicts acute and chronic toxicities for species across phyla, leveraging more data across different exposure duration whilst training the models.

Moreover, a model with adaptable exposure duration on the species level could in theory also be used for modelling species sensitivity distributions, which relate the concentration of a compound to the percentage of aquatic species (in a given ecosystem) that will be affected by that concentration.⁷

To build our aquatic toxicity models, we make use of the fact that QSAR tasks have very similar structures. The issue of aquatic toxicity prediction is split into many (often sparse) tasks: each task refers to a unique target species for which the effect is to be measured (see Figure 1).

For each species, several toxicity responses have been measured; these data provide the basis for our machine-learning approach.

While we aim to learn across tasks, the problem setup is defined in such a way that the unlabelled test instances (chemicals) for which we want to predict the LC50 values have not been observed for any of the other species before.

This poses a more challenging learning problem, where the learning algorithm has to generalize across structural properties of the molecule. This problem setup has the practical implication that we can predict the LC50 values for newly identified chemicals that have never before been tested on a given target species.

In summary, the proposed models are formally solving the following problem: given a set of chemicals $C = C_{train} \cup C_{test}$, where $C_{train} \cap C_{test} = \emptyset$, a compound $c \in C_{train}$, a duration $d \in \mathbb{R}^+$ and a target species $s \in S$, predict the lethal concentration of a new compound $c_{new} \in C_{test}$ for 50% of $s \in S$ after time duration d. Each compound is represented by a molecular embedding and physical-chemical features, whereas for each target species, taxonomical information on its phylum and class group is available.

OECD Validation Principles

With the heightened relevance of the QSAR models in the REACH legislation, the need for validated QSAR models of high quality has grown. Addressing this, the OECD principles⁵ present requirements that QSAR models fit for regulatory applications should adhere to. Although our work does not aim to present a model for regulatory purposes but rather aims to inform future development, we address these principles here.

First, to ensure that researchers can assess the potential use of a validated QSAR model, a well defined endpoint should be specified. In our work, we address endpoints in the category of ecological effects, which are included in the endpoints needed for regulatory assessment,⁵ more specifically the E/LC50 is used as the endpoint to be predicted. These endpoints are addressed in a 'general (Q)SAR model(s) based upon a common toxic effect'⁵ of aquatic



Figure 1: Aquatic toxicity QSAR tasks: The setup of the individual aquatic species tasks. The image shows how the tasks can be used for meta-learning: using the data in the training tasks to utilise additional data for the test task. Meta-learning methods can differ in the way these utilise the training task data.

species.

To define when a QSAR model may validly be employed, any QSAR model should include a description of the domain of applicability defined in the chemical structure space. This domain should be determined systematically to ensure that a model is not forced to extrapolate into unintended domains and is ideally defined prior to building a training set. Our work, however, addresses the issue that QSAR models are used outside of their applicability domain for low-resource datasets, which would not have enough resources to build a single task model on. Hence, we deliberately aim to develop a generally applicable model on given datasets by including different experimental durations and all applicable chemicals.

It is important to note that the training set of a QSAR model always induces a domain of applicability.⁵ Although measuring the domain of applicability is left as future work, it is interesting to note that toxicological datasets have natural biases. Under the REACH programme, for instance, chemicals of over 1 ton production volume need to be registered with toxicological information.⁸ Hence, datasets include biased information on chemicals that are produced at higher volumes, whereas chemicals under the threshold avoid testing, although their acute toxicity may be more concerning.⁸

Further, validated QSAR models need to be reproducible and transparent. To address this, we describe all employed algorithms, datasets and chemical descriptors and make these publicly available via a Git repository.⁴ In our work, black box models, specifically neural network models, are employed that are not transparent but are permitted via the OECD guidance document.

Finally, the performance of a QSAR model must be measured and validated soundly, paying special attention to robustness and predictive capacity. To assess the stability of predictions, we build partial models via cross-validation.⁵ The predictive capacity of our model is seen by its performance when extrapolating to an external held-out test set. All models are exclusively evaluated on the real-world challenge of predicting the toxicity of *previously unseen* chemicals, i.e., chemicals not used for training.

Related Work

In this section, we review work on QSAR-modelling specific for predicting aquatic toxicity, as well as advances in various types of meta-learning (including multitask learning) for QSARmodelling in general.

QSAR models for predicting Aquatic Toxicity

One of the simplest QSAR models proposed by the United States Environmental Protection Agency (USEPA) is ECOSAR – a regulatory model that uses a linear relationship between chemicals and their toxicity based on the octanol-water coefficient of the chemical. Based on building different linear regressions on groups of chemicals, ECOSAR is a non-species-specific tool for aquatic toxicity. Unfortunately, large safety factors need to be added to the predictions for their use in risk assessment.⁶

With the rise of machine learning, aquatic toxicity models, like other branches of QSAR modelling, have started using machine learning models built for singular tasks. Using machine learning models, the Toxicity Estimation Software Tool (T.E.S.T.) developed by the USEPA is a deployed set of QSAR predictors.⁹ Among other toxicity and physical-chemical attribute predictors, T.E.S.T. implements acute aquatic toxicity QSARs on three species, representing fish, daphnia and algae,⁹ utilising various methods, including hierarchical modelling and ensembles. Vega¹⁰ extends multiple linear regressions from T.E.S.T. but also implements more complex models.¹⁰ Zhou et al.¹¹ compares the performance of different open-source tools in classifying acute fish and daphnid toxicity.

Various extensions to these regulatory models have been proposed. Wu and Wei¹² applied multitask learning to a toxicity context, including oral rat toxicity and aquatic toxicity. Although the T.E.S.T. baseline compares well against the new methods, the multitask neural network and a combination of this method and gradient boosting trees perform well.¹² Alternatively, Lunghini et al.¹³ proposed to build a model for toxicity prediction of fish, daphnids, and algae, respectively, associating all assays only with the high-level category, such that the species of an assay cannot be determined anymore.

Considering available datasets from literature, all data points for a model were acquired using the same experimental setup, but instead of focussing on a single species per model, multiple species per high-level category were considered. Their model was shown to outperform ECOSAR, T.E.S.T., and Vega on a previously unseen industrial set of toxicity data. In contrast to these high-level models, Sheffield and Judson¹⁴ built an ensemble learner on a species level, predicting the toxicity of fish only.

Singh et al.⁶ propose a model that is trained on a given species but can extrapolate to different species in different classes. As such, the training set used consists of a single algae species, whereas the model is tested on an external set of said algae species, as well as on an unseen algae, daphnid and fish species, respectively.

Learning across tasks

Machine learning models typically require an abundance of labelled data. Meta-learning attempts to address this issue by asking *how to learn to learn tasks?* For this, meta-learning borrows intuition from how humans learn and solve problems. Instead of learning each task independently and anew, humans approach each challenge with prior knowledge.^{3,15}

With the success of transfer learning techniques in, e.g. natural language processing or image analysis, its potential use in QSAR modelling has been recognised.^{16,17} Erhan et al.¹⁸ first used a multitask neural network in their work on collaborative filtering. More specifically, they propose casting biological targets as users, molecular compounds as items, and the resulting biological activity as ratings. Dahl et al.¹⁹ utilised multitask learning to predict both biochemical (in test tubes) and cell type (in cell cultures) assays. Ramsundar et al.²⁰ predicted binary biological activity using 'massively' multitask neural networks built on over 200 tasks with over 40 million experimental values and varying endpoints. Sadawi et al.²¹ used multitask learning via random forest models previously shown to be effective in single-task cases.²² Using a subset of the ChEMBL dataset collection,²³ the tasks in their work concern the prediction of inhibitory and potency effects on target proteins; specifically, they predicted the concentration of compounds that results in a biological effect on the target protein. More recently, Olier et al.²⁴ proposed a transformational machine learning approach, which takes inspiration from multitask learning, transfer learning and ensemble learning. Using data from the ChEMBL dataset collection,²³ they predict multiple inhibitory effects on various target proteins. The approach aims to learn multitask-specific compound representations. This representation shares knowledge between all tasks, by encapsulating the general consensus on biological activity.

Our work aims to build a generally applicable species-level model to predict toxicity on 'any' aquatic species. Although Gajewicz-Skretna et al.²⁵ reported in a study for classifying aquatic toxicity that models built on a local chemical compound space performed better than ones for large chemical spaces, they agree with the added value of large models. Recent research has also evaluated the use of graphical features for compounds(e.g. ^{26,27}). Jiang et al. ²⁸, however, found that 'descriptor-based models outperform the graph-based models in the predictions of a variety of molecular properties in terms of predictive accuracy and computational efficiency'. Hence, molecular fingerprints in combination with physical-chemical attributes are used in our work.

To the best of our knowledge, this study is the first to build a generally applicable multispecies aquatic toxicity model across phyla for flexible exposure duration and on a large chemical applicability domain.

Data

This section presents the dataset used to make our QSAR aquatic toxicity models, of which the pre-processed version is available in our git repository.⁴ The ECOTOXicology Knowledgebase is a source for locating single chemical toxicity data for aquatic life, terrestrial plants and wildlife, which is maintained by the USEPA.²⁹

Using the ECOTOX data as integrated in the OECD QSAR toolbox,³⁰ a subselection of the entire database was created for modelling purposes. The final dataset used for modelling contained 24 816 aquatic toxicity values (LC50) altogether, for 351 different aquatic species and 2674 chemicals. Species are described only by their taxonomic position in classes and phyla, whereas chemicals have more descriptive features. The data is sparse, as many species have few chemicals tested on them (see Figure 2).

For our purpose, we have selected all experimental data that was represented as LC50 in the database, i.e., those concentrations giving 50% mortality at the end of the (indicated) test duration. We kept LC50 read-outs for all test durations, but we averaged the toxicity values that were produced using the chemical, the same species and identical test duration. Therefore, in the end, only one LC50 value was generated for any specific combination of chemical, species and test duration. This was considered necessary, as otherwise, some chemicals/species/duration combinations would be overrepresented and thus bias model training. As aquatic toxicity values have been gathered over decades in various laboratories, causing variation among experimental values, Lunghini et al.¹³ reported that the ecotoxicological dataset qualities heavily impact model performance – a concern also found in other work.^{31,32}



Figure 2: Dataset sizes and drug counts in the retrieved dataset. Both axes are on a log-scale.

Endpoint

The toxicity endpoint – the target variable – to be predicted by our models is the concentration of a chemical needed to trigger a certain toxic effect; here, we have selected 50% mortality (LC50, lethal concentration 50%), on one specific aquatic species, and after a specific test duration.

The LC50 values are standardised to $\frac{mg}{L}$ units where possible and dropped wherever not. Due to the spread of the LC50 target, we predict the real-valued $\log_{10}(LC50)$. Endpoints that indicate bounds (more than, less than, and in between) are disregarded. Higher bounds are due to detection limits of the toxicity experiments when, e.g., no more of the substance can be dissolved into the water, or when it is not practically useful to test with higher concentrations. The data with bounded LC50 values could serve as a very useful validation set for toxicity models.

Preprocessing

Each database entry contains the concentration of a specific toxicity endpoint (in our case LC50), which corresponds to a unique combination of species, chemical and duration. Experiments performed under the same experimental conditions (same chemical, same species, same duration) multiple times, are averaged into one result using the empirical mean, as suggested by the REACH guidance document.⁵ We note that by combining multiple toxicity targets for the same experiment, the variance of the experiments is no longer captured, and noise can be added to the data.

Each of the 351 species is grouped into taxonomies via 20 classes and 9 phyla. With the large majority of species belonging to either the Chordata or Arthropoda phylum, this dataset is well suited for predicting the endpoints needed for chemical regulation.⁵ As the toxicity is to be predicted on a species level, any subspecies of a species were combined into one species via their empirical mean.

It was ensured that the chemicals are uniquely identified via their SMILES (Simplified Molecular-Input Entry-System) representation. The SMILES were examined to ensure that chemicals not suited for modelling were removed. In this process, SMILES referring to inorganic chemicals (metals or metal salts) and metallo-organic chemicals were excluded. The presence of metals or metal salts is often responsible for the majority of the observed toxicity. Other chemicals that could not be represented by a single SMILES (e.g., mixtures or natural extracts) were also omitted. To ensure that the SMILES representation is consistent for all chemicals, Kekulé SMILES are used, as produced by the Open-source QSAR-ready chemical structure standardization workflow³³ The consistent SMILES representation ensures that all chemical descriptors and fingerprints are derived in the same fashion – regardless of how the

original SMILES was created (e.g., the SMILES produced by the OECD QSAR Toolbox).

Although it is common to specify one experiment type (and one exposure duration) to use for modelling, our work aims to build a large applicability domain model, enabling the methods to learn across various duration times. Thus, similar to the work of Sheffield and Judson,¹⁴ all experimental setups are included in the dataset and are defined by their duration. With this, short-term (acute) and long-term (chronic) toxicity can be modelled together. As acute and chronic periods vary for each species, the duration is a real-valued feature. Duration values are converted into days wherever possible and disregarded wherever a duration is not specified. In the light of building a generally applicable model with few restrictions, no outlier removal was performed.

Chemical Descriptors

Although recent research has evaluated the use of graphical features for compounds, our work uses chemical embeddings based on Jiang et al.'s finding that descriptor-based models outperform graph-based models in the predictions of a variety of molecular properties in terms of predictive accuracy and computational efficiency'.²⁸ We thus rely on chemical fingerprints and relevant physical-chemical properties.

Fingerprints are embeddings that aim to capture two-dimensional chemical structures. Our work uses circular fingerprints called extended connectivity fingerprints (ECFP), which were specifically designed for QSAR modelling.³⁴ Our work uses the original 1024-bit binary ECFP4 fingerprints, which aim to capture precise atom environment sub-structural features with a radius of 2.³⁴ The fingerprints are calculated from their SMILES representation using the open-source RdKit.³⁵

As certain physical-chemical attributes may also yield important information on a molecule, relevant physical-chemical attributes were gathered from PaDEL.³⁶ The attributes gathered were suggested by a domain expert, and include constitutional and hydrophobic attributes. We performed simple feature selection, as well as added missing value indicators, in case PaDEL did not have the values for a given chemical.

Finally, the structural properties included are counts of atom types, rings, hydrogen bond donors, acceptors, as well as the molar refractivity, polarizability, ionization energy and topological polar surface area of the molecule.

Attributes that are expected to be specifically related to aquatic toxicity are the logarithm of the octanol-water partition coefficient, $logk_{ow}$ or log P, the octanol/air partition coefficient KOA, and the pH dependent octanol-water distribution coefficient, logD5.5 and logD7.4, in addition to the vapour pressure and the water solubility of a molecule.

Methodology

In this section, the QSAR solutions we considered are elaborated further. We put additional care into optimizing the hyperparameters of each method, which is detailed in the supplementary material.³⁷ The solutions were implemented using Scikit-learn,³⁸ Pytorch³⁹ and deepChem.⁴⁰

Single-task Models

The single-task models approach each dataset individually without using any knowledge of other datasets. As such, they cannot make use of data on other species or their taxonomies.

Single-task Mean

The single-task mean model predicts the mean of training set toxicity values for a given species in training. This is considered a simple baseline: Any model that utilises additional information should be able to outperform this prediction.

Single-task Random Forest

Random forest models are ensemble models that predict the consensus value across multiple decision trees.^{41,42} Other toxicology studies have found them the best performing single-task model.²² Independent random forest models are fitted for each species using the molecular descriptors and the exposure duration as features, as illustrated in Figure 3a.



(a) Single-task Model: fitted on data from $a \ single$ target species

(b) Multitask Model: fitted on data from *all* species with additional taxonomic info.

Figure 3: Schematic overview of random forest models. The endpoint value is represented as 'Y'.

Multitask Learning Models

The multitask learning models learn the separate tasks jointly to share knowledge between them during training. These models can utilise data from different species and make use of features capturing taxonomic information, i.e., species, phyla, and class as categorical variables.

Multitask Mean

The multitask mean predicts the mean toxicity value of all species seen in training.

Multitask Random Forest

In the multitask random forest model, a single random forest is trained on data from all species, with additional taxonomic information making it possible to give different predictions for different aquatic species (see Figure 3b). The higher-order taxonomy levels may improve the model's performance if similar species respond similarly (Sadawi et al.).

Multitask Stacked Ensemble Learner

Sheffield and Judson proposed the stacked ensemble learner, which creates an ensemble from different models by learning how to best combine their predictions. They used linear regression to combine three base models: support vector regression, gradient boosted trees and a random forest. All base learners use the molecular descriptors, taxonomic information and exposure duration.



Figure 4: Stacked Ensemble Learning: base learners are combined into one consensus value.

Multitask Neural Networks

We consider two distinct neural network architectures.

One Output Node. The neural network is trained on all of the tasks, but uses only one node in the output layer, see Figure 5a. In addition to chemical descriptors and exposure duration features, including the taxonomic information allows predicting a different toxicity value for different species. We refer to this model as neural network.

Multiple Output Nodes. The *multitarget* neural network predicts the toxicities of all n tasks using n output nodes, see Figure 5b. This allows the neural network to share



(a) All aquatic species are predicted via the one output node.

(b) Schematic overview of multitarget neural network: One output node per species.

Figure 5: Multitask Neural Networks

the internal feature extraction and representation part embedded in the hidden layers of the neural network, whereas the task-specific dependencies can be captured in the weights toward the task-specific output nodes.

Transformational Machine Learning



(a) Transformational Embedding: representation of a chemical is the toxicity predicted by all of the single models.

(b) Final model: Train a single-task model using transformational embeddings as chemical features.

Figure 6: Transformational Machine Learning.²⁴

Transformational Machine Learning (TML)²⁴ combines aspects of ensemble-, multitask-, and transfer learning. It can be split into two parts:

- 1. Create a shared representation of the compound: A single-task random forest is fitted for each target species. Once all single-task models have been built, they predict the toxicity of a specific compound for all species, as shown in Figure 6a. These predictions are then placed in a vector, which will be our representation for the compound.
- 2. Build final single-task models: A single-task random forest model is fitted for all target species, respectively, but the input features are now the representations from Step 1, see Figure 6b. By training a single-task random forest for a given species, the model can learn to use the general consensus over similar species in the vector.

We use two models: the one described above (TML) and one aggregating this prediction with the single-task random forest model trained in the first step $(TML \ Stacked)$.

Fine-tuning

Fine-tuning techniques are a simple way to perform transfer learning with neural networks.⁴³ First, a neural network is trained on all tasks to extract knowledge from the input features and build an internal representation; then, (a selection of) the weights are adapted to the final task. In our case, a neural network is trained on all species, before the head of the network is trained on the given aquatic species.

Model Agnostic Meta-Learning

Model Agnostic Meta-Learning (MAML)⁴⁴ is a model-agnostic transfer learning technique. We use it with a neural network. The initialization weights of a standard neural network are random values and require a substantial amount of training data to adapt for a given task. MAML aims to encapsulate knowledge from related tasks into good initialisation parameters. It observes which weights worked well for related tasks to suggest initial weights that can be quickly adapted to a new task. In contrast to fine-tuning, which adapts weights found optimal for all tasks to a single-task, MAML aims to find initialisation weights that allow for quick adapting to all tasks,⁴⁵ as illustrated in Figure 7.



Figure 7: Intuition behind MAML:⁴⁴ Let the model used have initialization parameter vector $\overline{\theta}$. The blue points show the optimal configuration of initialization parameters $\overline{\theta}^{(1)}, \overline{\theta}^{(2)}, \overline{\theta}^{(3)}, \overline{\theta}^{(4)}$ for specific species tasks 1-4. MAML aims to find $\overline{\theta}^*$, such that the optimal configuration for each task can be reached equally fast.⁴⁵

Experiments

In the following, we examine the prediction quality of QSAR algorithms on new chemical compounds for which no observations (assays) were used during training. For our experiments, therefore partition the ECOTOX dataset uniformly at random into *training chemicals*, which are used for training our models, and *test chemicals*, which are used for assessing their quality. This scheme is illustrated in Figure 8, with test assays shown in dark blue; duration times are omitted for simplicity.

We address the following research questions:

R1 What is the average prediction performance of the previously discussed (hyperparameter optimized) QSAR algorithms on previously unseen chemicals?



Figure 8: Training vs testing data: The rows represent chemicals, whereas the columns represent the study species. Our training and testing data consist of disjoint subsets of chemicals.

- R2 How does the performance of the models (both single-task and multitask) increase when exposed to more data from the target species?
- R3 How does the performance of the models increase when more data from other species (to learn across datasets) is available?

Prediction performance is measured in terms of the root mean squared error (RMSE)

$$RMSE = \sqrt{\sum_{i=1}^{n} \frac{(\hat{y}_i - y_i)^2}{n}},$$
(1)

where \hat{y}_i is the *predicted* and y_i is the *true* label for the *i*-th out of the *n* test assays over which the metric is being computed. The performance error is calculated per species/ chemical/ fold and averaged over all species/ chemicals/ folds.

In addition, a Friedman test⁴⁶ is used according to the suggestion by Demšar⁴⁷ to determine the statistical significance of performance differences among multiple algorithms. We test whether and to what extent any pair of algorithms statistically differ in performance; we refer to our supplementary material for details.

Average Prediction Performance of QSAR Algorithms

To properly assess the prediction performance of the QSAR algorithms, we proceeded as follows. According to the above splitting scheme, we allocated 80% of the chemicals for training and 20% for testing; we call the respective portions of the ECOTOX dataset the *internal* and *external* folds. Then, two types of experiments were conducted. The first assesses the predictive capacity of each hyperparameter-optimised QSAR algorithm trained on the internal fold when extrapolating to the external fold.

The second experiment assesses the stability of each QSAR algorithm via cross-validation. To this end, the *chemicals* contained in the internal fold were partitioned into 5 disjoint and equally sized sub-folds (each one containing 20% of the chemicals). We built 5 hyperparameteroptimised partial models that exclude a sub-fold from the training set to subsequently predict.

This process was repeated three times with different partitions, yielding 15 estimates for each QSAR algorithm.

Results

Figure 9 shows different RMSE performances of the QSAR algorithms. Plot 9a and 9b show the RMSE of the hyperparameter-optimized algorithms on the external test fold, once aggregated across species and once across (test) chemicals. These numbers, therefore, give an unbiased estimate of the out-of-sample prediction performance of the models.

The best-performing methods are the multitask random forest and the stacked ensembling method. Aggregating over chemicals, their mean test RMSEs are 1.07 and 1.08, respectively. The differences between the techniques are mostly statistically significant; we refer to the supplement for details.

Predictions with an RMSE of less than 1 are within a factor 10 of the original LC50 value (before applying the log-scale), which makes such models useful for various applications when certain error margins are applied, including risk-assessments of regulators; refer to the

supplement for a derivation.

The results in plot 9b show that the *median* RMSE of several methods is indeed below 1, so at least for a significant portion of chemicals, the methods can be considered to work acceptably or even very well: The two previously mentioned techniques are the only ones with a 25% quantile below 0.5.

Plot 9c summarises, for each of the algorithms, the 15 validation results of the internal hyperparameter optimisation procedure; it hence reflects the stability of the performances (narrow boxplots indicate high stability of the procedure and thus that the results in Plot 9a and 9b are close to the true average results). Plot 9c underlines that these results can be considered largely stable. For most methods, the performance only changes marginally with the chemicals selected for training. The only exception is MAML, which is too unstable for use, but does not perform competitively under any observed condition anyway.



(c) RMSE on internal folds.

Figure 9: Comparison of Prediction Performances (RMSE) of different algorithms.

Prediction Performance as a Function of Number of Assays

Experiment Setup

Addressing research question R2, we now study the effect of more data on the target species. For this, we utilise learning curves for each of the algorithms.⁴⁸ First, the ECOTOX database was randomly uniformly split using 90% of the chemicals for training and 10% for testing. We then identified all species for which at least 128 training assays were available (with the goal to form reasonably long useful learning curves). The 35 species that satisfied this criterion are called the *study species*. For the remaining species (with few assays), training assays were moved into an *auxiliary data set*, and test assays were removed entirely from the data set. Finally, learning curves in the form of RMSE as a function of the number of training assays (per species) were computed.

We built the learning curves as follows: For each *anchor* (training set size) $s \in \{\lfloor \sqrt{2^n} \rfloor \mid n \in \{2, ..., 14\}\}$, all of the QSAR algorithms were trained using the training assays and then the RMSE was computed on the test assays. The number of assays used at s was s for each model in a single-task learner and $35 \cdot s$ (with s samples from each of the 35 study species) for multi-task learners. The assays used at previous anchors were included in the following anchors, e.g., the assays used at the anchor utilizing 5 assays were also used for training at the following anchors utilizing 8, 11, 16 assays and so on. To reduce the effect of selecting the assays in a certain order, we built not only one but *three* such curves with different assays order and then averaged.

With this, we now elaborate on how the models perform when more data is being presented in two different settings. In the first case, only assays from the 35 study species were used for training. In the second case, *all* the (10 200) assays from the auxiliary data set (remaining species) were used in addition during training at each anchor. Figure 10 shows a schematic overview of both setups.



Figure 10: Study Setup: Using 35 study species in our train and test set, a harsh low-resource situation is simulated with the training set containing only the downsampled species, whereas the second scenario adds the remaining assays from other species to the training set too.

Results

The plots in Figure 11 show learning curves without (left) and with (right) auxiliary data available for training. In the top row, the RMSE is computed for each species, and the curves aggregate the species-wise errors, whereas the bottom row aggregates over chemicals.

Lines show mean values and shaded areas the 90% confidence bands computed from 1 000 bootstrap samples.

Looking at the left plots, it can be seen that the advantage of the two multitask methods – i.e., the multitask random forest and ensemble stacking – are rather independent of the number of assays used for training. The curves are constantly below the others, so these two algorithms are constantly the best choices, no matter how many training examples are being used.

An even more important observation is that all curves are significantly dropping throughout the entire interval under study, including the 128 anchor. A first implication is that all the QSAR algorithms indeed exhibit an ability to *learn* to predict LC50 from the ECOTOX data (otherwise curves would plateau immediately). Second, the fact that curves keep drop-



Figure 11: Learning curves showing the effect of downsampling the study species without (left) and with (right) auxiliary species available for training. Once grouped over species (top row) and once over chemicals (bottom row).

ping significantly at anchor 128 suggests that it might be fairly possible to predict LC50 even with a *satisfactory* RMSE below 1.0 if more assays were available.

The right plots suggest that auxiliary assays are advantageous if and only if very few species-specific assays are available. The general observation across all multi-task learning algorithms is that the learning curves start off better but decrease less steeply. The first implication is that, if less than roughly 20 training assays are available for a species, it is likely that the random forest or stacking ensemble can benefit from the auxiliary assays. In those common, low-resource cases, using a neural network (with or without finetuning) will do better than learning only with the assays from the study species alone. However, the second implication is that, if more assays are available for the study species, it seems better to ignore auxiliary assays, since they seem to slow down the learning process. This holds at least for random forests and stacking ensembles, both of which show better performance at the 128 anchor when no auxiliary species are being used. Additionally, TML is dependent on all of its single-task models' performances, as well as the length of its representation here. If so many assays are available and if a neural network is used, the auxiliary species should be used, and the network should not be fine-tuned on the study species. However, given the slope of the learning curves, with 128 assays or more, it seems best to just use a random forest or stacking ensemble without auxiliary assays.

Prediction Performance as a Function of Number of Species

In this learning curve experiment, we investigate research question R3: to what extent does the number of species included in the training sets affect the performance of multi-task models?

First, the ECOTOX database was split as outlined previously, using 75% of the chemicals for training and 25% for testing. Second, we identified all the species for which there are at least three chemicals among the test assays.

The resulting 180 species are the *study species*; this set happened to be disjoint from the 35 previous study species. Third, to assure a reasonable number of training instances, among the remaining species, we identified the ones with at least 64 training assays. The resulting 64 species (coincidentally, there were 64 species as well) are called the *auxiliary species*. The assays for all the other species were discarded.

To determine the learning curves, we proceeded as follows. First, the number of assays per auxiliary species was down-sampled to 64. This was done, because the number of samples per auxiliary species varied from 64 to over 1 000, so a change in a performance curve could have been attributed to the fact that many data samples were added to the training set, and not primarily to the addition of additional species to infer knowledge from. Second, a random permutation of the auxiliary species was created. Third, for each study species, the RMSE for each QSAR algorithm was computed on the test assays when using the respective training assays and the 64 training assays from each of the $|\sqrt{2^n}|$ first auxiliary species, where $n \in \{1, 2, ..., 12\}$, for training. The experiments were repeated over 3 different pseudo-random number seeds, inducing different down-sampled auxiliary datasets and different permutations of the auxiliary species. The general experimental setup is schematically shown in Figure 12.



Figure 12: Meta-learning curve: Iterating over 180 study species, a study species with its training and test set, is selected. Sampling 0,2,4...,64 auxiliary species into the training set, a new QSAR model is built. With this, the impact of adding more species to aid in learning a study species is shown.

Results

Figure 13 shows the performances, with the left plot aggregating over species and the right over chemicals. Note that single-task models have been omitted, as they do not make use of additional data.

To answer the research question R2, we observe that the benefit of additional training assays from other species is only significantly beneficial for NN with one output unit and for Finetuning-Top. The curves of the other algorithms have a shallow improvement or even partially deteriorate (e.g., Multitask RFs when averaging over species). For these two algorithms, the additional data though does have a rather interesting effect. At the highest anchor (64 additional species), Finetuning-Top achieves the best results when averaging over species, and the NN with one output is not outperformed when averaging over chemicals.

More importantly, both algorithms still show significant learning progress at that point on the curve. In other words, one might conjecture that adding assays from additional



Figure 13: Meta-learning curves showing the effect of adding more auxiliary species to the training set of a study species. Results averaged over species (left) and chemicals (right).

species would lead to overall results superior to those of other learners and possibly lead to results below the 1.0 RMSE threshold.

However, these assessments must be viewed with caution. The test matrix for the defined over the test chemicals and the 180 study species is extremely sparse, which has several side effects. Firstly, TML is now working consistently better than on the 35 study species of the previous learning curve even though it only marginally improves with increasing additional training assays from other species. Hence, TML behaves very differently on the species/chemical combinations analysed in this experiment than in the previous one.

Secondly, the two previous best models (multitask random forest and stacking ensemble) also perform very well in this setup when averaging over chemicals, but not when averaging over species. This is caused by a single chemical for which prediction qualities are low for most species, and, due to the sparsity of test data, this has a high influence when averaging over species, but a low influence when averaging over chemicals – in other words, the results are very sensitive to the species/chemical combinations used for training and testing respectively (details can be found in the supplementary material).

A further hypothesis addressing these differences may be different instance weightings between single- and multi-task models. To achieve a generally good performance, a multitask model aims to predict the majority of assays well. Due to the large differences in the number of assays with a certain chemical or species, the multitask model may aim to predict the largest groups of chemicals or species better. A single-task model, however, could concentrate on each species more equally, as a separate model is built for each task. The single-task models optimize for good performance over species, whereas when the models are averaged over chemicals the single-task models are not as good as the multitask model. Future work should investigate how the choice of evaluation affects the relative order and, further, it may be interesting to experiment with instance weighting explicitly by weighting training instances whilst building a model.

Overall, the results motivate future work in which the selection of species and chemicals is studied further. Learning across certain more related tasks (species or chemicals), that were more carefully selected, may further benefit model performance. An alternative could be adding more detailed, scaled-task-relatedness measures to replace the categorical species taxonomies.

In the sense of meta-learning, this could motivate a context-based approach, in which the learning algorithm itself is chosen based on the properties of the species and/or the chemicals for which training instances are available or predictions need to be made, as is done in the work of Olier et al..²²

Discussion

Our work has addressed modelling LC50 values (mortality rate in 50% of the experiments) of different aquatic species, specifically using a collection of well-known sparse ecotoxicological datasets.

To make predictions for species with few assays, we explore the use of different machinelearning techniques to leverage additional data from other species.

We pay special attention to addressing domain-specific requirements via the OECD principles, and we evaluate the models in a setting where we make predictions for the toxicity of species for a chemical that has not been seen before for any of the other species. This is motivated by the fact that this is the most common use-case of toxicological predictions, which can be readily applied when a new chemical needs to be evaluated.

Based on our experiments, for this problem setting, we advise the use of the multitask random forest model. Its performance is stable, as seen in the internal validations, and the performance is good on external validations, both averaged over chemicals and species. Furthermore, the multitask model also performs well in simulated low-resource situations. When looking at the general datasets consisting of all assays, there is no statistical evidence that the multitask random forest performs better than the single-task random forest. The multitask random forest model has a lower performance error than its single task version in 54% of unseen chemicals. However, when examining cases, in which there were less than 5 seen compounds for a species, the multitask random forest outperforms the single task random forest in 80% of unseen chemicals. Extrapolating onwards from the learning curve experiments, the neural network with one output unit seems promising with more assays available.

As we believe that the inclusion of class and phyla information aids the multitask models, we hypothesise that a continuous distance measure between the species could further enhance these models. Therefore, in future work, different, potentially more easily obtainable measures of target relatedness could be investigated. Furthermore, our investigation into low-resource situations via learning curves has given more insight into individual approaches. A future investigation could evaluate the effect of selecting chemicals and species with more care.

To conclude, we successfully present multitask models on a species level which predict toxicity on flexible exposure duration and a large chemical applicability domain, showing promising results for models with general chemical applicability as well as applicability across phyla. With this research, we hope to not only take a step towards mitigating the need for in vivo experiments but also hope to inspire the use of knowledge-sharing approaches for other low-resource QSAR problems.

Supporting Information Available

Supplementary Material:

- Hyperparameter Optimisation,
- Statistical Significance between algorithms on the average prediction performance
- The influence of data sparsity in the learning curve performances
- Performance on real low resource tasks

References

- Cherkasov, A.; Muratov, E. N.; Fourches, D.; Varnek, A.; Baskin, I. I.; Cronin, M.; Dearden, J.; Gramatica, P.; Martin, Y. C.; Todeschini, R.; others QSAR modeling: Where have you been? Where are you going to? *Journal of Medicinal Chemistry* 2014, 57 (12), 4977–5010.
- (2) Gramatica, P. Principles of QSAR models validation: internal and external. QSAR &
 Combinatorial Science 2007, 26 (5), 694–701.
- (3) Brazdil, P.; van Rijn, J. N.; Soares, C.; Vanschoren, J. Metalearning: Applications to Automated Machine Learning and Data Mining, 2nd ed.; Springer, 2022.
- (4) Schlender, T. Code Repository of "The Bigger Fish Aquatic Toxicity QSAR models". https://github.com/ADA-research/TheBiggerFish.
- (5) OECD Guidance Document on the Validation of (Quantitative) Structure-Activity Relationship [(Q)SAR] Models; 2014.
- (6) Singh, K. P.; Gupta, S.; Kumar, A.; Mohan, D. Multispecies QSAR Modeling for Predicting the Aquatic Toxicity of Diverse Organic Chemicals for Regulatory Toxicology. *Chemical Research in Toxicology* **2014**, *27* (5), 741–753.

- (7) Fox, D.; van Dam, R.; Fisher, R.; Batley, G.; Tillmanns, A.; Thorley, J.; Schwarz, C.; Spry, D.; McTavish, K. Recent Developments in Species Sensitivity Distribution Modeling. *Environmental Toxicology and Chemistry* **2021**, *40* (2), 293–308.
- (8) Wandall, B.; Hansson, S. O.; Rudén, C. Bias in toxicology. Archives of Toxicology 2007, 81 (9), 605–617.
- (9) Martin, T. Toxicity estimation software tool (TEST). U.S. Environmental Protection Agency, 2016.
- (10) Benfenati, E.; Manganaro, A.; Gini, G. C. VEGA-QSAR: AI Inside a Platform for Predictive Toxicology. Proceedings of the Workshop Popularize Artificial Intelligence co-located with the 13th Conference of the Italian Association for Artificial Intelligence (AI*IA 2013). 2013; pp 21–28.
- (11) Zhou, L.; Fan, D.; Yin, W.; Gu, W.; Wang, Z.; Liu, J.; Xu, Y.; Shi, L.; Liu, M.; Ji, G. Comparison of seven in silico tools for evaluating of daphnia and fish acute toxicity: case study on Chinese Priority Controlled Chemicals and new chemicals. *BMC Bioinformatics* **2021**, *22 (151)*, 1–31.
- (12) Wu, K.; Wei, G.-W. Quantitative Toxicity Prediction Using Topology Based Multitask Deep Neural Networks. Journal of Chemical Information and Modeling 2018, 58 (2), 520–531.
- (13) Lunghini, F.; Marcou, G.; Azam, P.; Enrici, M.; Van Miert, E.; Varnek, A. Consensus QSAR models estimating acute toxicity to aquatic organisms from different trophic levels: algae, Daphnia and fish. SAR and QSAR in Environmental Research 2020, 31 (9), 655–675.
- (14) Sheffield, T. Y.; Judson, R. S. Ensemble QSAR Modeling to Predict Multispecies Fish Toxicity Lethal Concentrations and Points of Departure. *Environmental Science & Technology* 2019, 53 (21), 12793–12802.

- (15) Lake, B. M.; Ullman, T. D.; Tenenbaum, J. B.; Gershman, S. J. Building machines that learn and think like people. *Behavioral and Brain Sciences* 2017, 40.
- (16) Simoes, R. S.; Maltarollo, V. G.; Oliveira, P. R.; Honorio, K. M. Transfer and Multi-task Learning in QSAR Modeling: Advances and Challenges. *Frontiers in Pharmacology* 2018, 9 (74).
- (17) Cai, C.; Wang, S.; Xu, Y.; Zhang, W.; Tang, K.; Ouyang, Q.; Lai, L.; Pei, J. Transfer Learning for Drug Discovery. *Journal of Medicinal Chemistry* **2020**, *63* (16), 8683– 8694.
- (18) Erhan, D.; L'Heureux, P.; Yue, S. Y.; Bengio, Y. Collaborative Filtering on a Family of Biological Targets. Journal of Chemical Information and Modeling 2006, 46 (2), 626–635.
- (19) Dahl, G. E.; Jaitly, N.; Salakhutdinov, R. Multi-task Neural Networks for QSAR Predictions. CoRR 2014, abs/1406.1231.
- (20) Ramsundar, B.; Kearnes, S.; Riley, P.; Webster, D.; Konerding, D. E.; Pande, V. S.
 Massively Multitask Networks for Drug Discovery. *CoRR* 2015, *abs/1502.02072*.
- (21) Sadawi, N.; Olier, I.; Vanschoren, J.; van Rijn, J. N.; Besnard, J.; Bickerton, R.; Grosan, C.; Soldatova, L.; King, R. D. Multi-task learning with a natural metric for quantitative structure activity relationship learning. *Journal of Cheminformatics* 2019, 11 (1), 1–13.
- (22) Olier, I.; Sadawi, N.; Bickerton, G. R.; Vanschoren, J.; Grosan, C.; Soldatova, L.; King, R. D. Meta-QSAR: a large-scale application of meta-learning to drug design and discovery. *Machine Learning* **2018**, *107 (1)*, 285–311.
- (23) Gaulton, A.; Hersey, A.; Nowotka, M.; Bento, A. P.; Chambers, J.; Mendez, D.; Mu-

towo, P.; Atkinson, F.; Bellis, L. J.; Cibrián-Uhalte, E.; others The ChEMBL database in 2017. *Nucleic Acids Research* **2017**, *45 (D1)*, D945–D954.

- (24) Olier, I.; Orhobor, O. I.; Dash, T.; Davis, A. M.; Soldatova, L. N.; Vanschoren, J.; King, R. D. Transformational machine learning: learning how to learn from many related scientific problems. *Proceedings of the National Academy of Sciences* 2021, 118 (49).
- (25) Gajewicz-Skretna, A.; Gromelski, M.; Wyrzykowska, E.; Furuhama, A.; Yamamoto, H.; Suzuki, N. Aquatic toxicity (Pre)screening strategy for structurally diverse chemicals: global or local classification tree models? *Ecotoxicology and Environmental Safety* 2021, 208 (111738).
- (26) Altae-Tran, H.; Ramsundar, B.; Pappu, A. S.; Pande, V. Low data drug discovery with one-shot learning. ACS Central Science 2017, 3 (4), 283–293.
- (27) Nguyen, C. Q.; Kreatsoulas, C.; Branson, K. M. Meta-learning GNN initializations for low-resource molecular property prediction. ICML 2020 Workshop on Graph Representation Learning and Beyond. 2020.
- (28) Jiang, D.; Wu, Z.; Hsieh, C.-Y.; Chen, G.; Liao, B.; Wang, Z.; Shen, C.; Cao, D.; Wu, J.; Hou, T. Could graph neural networks learn better molecular representation for drug discovery? A comparison study of descriptor-based and graph-based models. *Journal of Cheminformatics* **2021**, *13* (1), 1–23.
- (29) Olker, J. H.; Elonen, C. M.; Pilli, A.; Anderson, A.; Kinziger, B.; Erickson, S.; Skopinski, M.; Pomplun, A.; LaLone, C. A.; Russom, C. L.; others The ECOTOXicology Knowledgebase: A Curated Database of Ecologically Relevant Toxicity Tests to Support Environmental Research and Risk Assessment. *Environmental Toxicology and Chemistry* **2022**, *41* (6), 1520–1539.

- (30) OECD OECD QSAR Toolbox. www.oecd.org/chemicalsafety/risk-assessment/ oecd-qsar-toolbox.html.
- (31) Thomas, P. C.; Bicherel, P.; Bauer, F. J. How in silico and QSAR approaches can increase confidence in environmental hazard and risk assessment. *Integrated Environ*mental Assessment and Management **2019**, 15 (1), 40–50.
- (32) Raimondo, S.; Jackson, C. R.; Barron, M. G. Influence of Taxonomic Relatedness and Chemical Mode of Action in Acute Interspecies Estimation Models for Aquatic Species. *Environmental Science & Technology* 2010, 44 (19), 7711–7716.
- (33) Mansouri, K.; Grulke, C.; Judson, R.; Richard, A.; Williams, A.; Kleinstreuer, N. Opensource QSAR-ready chemical structure standardization workflow. 19th International Workshop on (Quantitative) Structure-Activity Relationships in Environmental and Health Sciences. 2021.
- (34) Rogers, D.; Hahn, M. Extended-Connectivity Fingerprints. Journal of Chemical Information and Modeling 2010, 50 (5), 742–754.
- (35) RDKit Open-source cheminformatics. https://www.rdkit.org.
- (36) Yap, C. W. PaDEL-descriptor: an open source software to calculate molecular descriptors and fingerprints. *Journal of Computational Chemistry* 2011, 32 (7), 1466–1474.
- (37) Hutter, F., Kotthoff, L., Vanschoren, J., Eds. Automated machine learning methods, systems, challenges; Springer, 2019.
- (38) Pedregosa, F. et al. Scikit-learn: Machine Learning in Python. Journal of Machine Learning Research 2011, 12, 2825–2830.
- (39) Paszke, A. et al. PyTorch: An Imperative Style, High-Performance Deep Learning Library. Advances in Neural Information Processing Systems 32. 2019; pp 8024–8035.

- (40) Ramsundar, B.; Eastman, P.; Walters, P.; Pande, V.; Leswing, K.; Wu, Z. Deep Learning for the Life Sciences: Applying Deep Learning to Genomics, Microscopy, Drug Discovery, and More; O'Reilly Media, 2019.
- (41) Ho, T. K. Random decision forests. Third International Conference on Document Analysis and Recognition ICDAR 1995. 1995; pp 278–282.
- (42) Breiman, L. Random Forests. Machine learning 2001, 45 (1), 5–32.
- (43) Chen, W.-Y.; Liu, Y.-C.; Kira, Z.; Wang, Y.-C. F.; Huang, J.-B. A Closer Look at Few-shot Classification. International Conference on Learning Representations. 2019.
- (44) Finn, C.; Abbeel, P.; Levine, S. Model-Agnostic Meta-Learning for Fast Adaptation of Deep Networks. Proceedings of the 34th International Conference on Machine Learning. 2017; pp 1126–1135.
- (45) Huisman, M.; van Rijn, J. N.; Plaat, A. A survey of deep meta-learning. Artificial Intelligence Review 2021, 54 (6), 4483–4541.
- (46) Friedman, M. A comparison of alternative tests of significance for the problem of m rankings. The Annals of Mathematical Statistics 1940, 11 (1), 86–92.
- (47) Demšar, J. Statistical Comparisons of Classifiers over Multiple Data Sets. The Journal of Machine Learning Research 2006, 7, 1–30.
- (48) Mohr, F.; van Rijn, J. N. Learning Curves for Decision Making in Supervised Machine Learning – A Survey. CoRR 2022, abs/2201.12150.